

PMMA layer is not used; oxygen or moisture at grain boundaries provides quenching sites. The fast decay is related to trap-assisted recombination at grain boundaries, whereas the slow decay is related to radiative recombination inside the grains (fig. S9) (32).

This proposition was supported by analyzing the change in τ and f of MAPbBr₃ films with varying stoichiometric ratio. As MABr:PbBr₂ increased from 1:1 to 1.05:1, the average lifetime τ_{avg} gradually increased from 12.2 to 51.0 ns (table S5). The short τ_{avg} (12.2 ns) in the film with MABr:PbBr₂ = 1:1 originated from the substantial reduction in τ_2 . This implies that uncoordinated metallic Pb atoms at grain boundaries inhibit radiative recombination and cause strong non-radiative recombination (fig. S9). The MAPbBr₃ films fabricated with PbBr₂-rich perovskite solution (MABr:PbBr₂ = 1:1.05) had a longer lifetime than films with MABr:PbBr₂ = 1:1, possibly through PbBr₂-induced surface passivation (31). We calculated the average L_D using a model similar to that in a previous report (fig. S10) (33). The films (MABr:PbBr₂ = 1.05:1) underneath a PMMA layer exhibited a much smaller L_D (67 nm) than those previously reported (>1 μm) (34). We attribute this reduction in L_D to the reduced grain sizes in which excitons are under stronger spatial confinement, thereby reducing dissociation and enhancing radiative recombination; this compensates the plausible adverse effect of larger grain boundary area (6).

The PeLED fabricated from the MAPbBr₃ solution (MABr:PbBr₂ = 1:1) without using NCP showed poor luminous characteristics (maximum CE = 2.03×10^{-3} cd A⁻¹), mainly owing to high leakage current (fig. S11). In contrast, maximum CE was substantially increased (0.183 cd A⁻¹) when a full-coverage uniform MAPbBr₃ nanograin layer (MABr:PbBr₂ = 1:1) with decreased grain size was achieved with S-NCP, without stoichiometric modifications to avoid metallic Pb atoms (Fig. 4, A and B, and Table 1). The maximum CE was boosted to 21.4 cd A⁻¹ in the PeLEDs fabricated with perovskite solutions with excess MABr (1.07:1, 1.05:1, 1.03:1 and 1.02:1) (Fig. 4A and Table 1). As MABr:PbBr₂ increased from 1:1 to 1.05:1, the maximum CE varied from 0.183 to 21.4 cd A⁻¹.

We further increased the CE of PeLEDs by using A-NCP. The PeLEDs based on A-NCP had a maximum CE of 42.9 cd A⁻¹ (Fig. 4, C and D, and Table 1), which represents an EQE of 8.53% when the angular emission profile is considered (fig. S12). The EL spectra of PeLEDs were very narrow; full width at half maximum was ~20 nm for all spectra. This high color purity of OIP emitters shows great potential when used in displays (Fig. 4E). A pixel of the PeLED based on MABr:PbBr₂ = 1.05:1 exhibited strong green-light emission (fig. S13A). Furthermore, the proposed processes and materials used therein are compatible with flexible and large-area devices; a high-brightness flexible PeLED (Fig. 4, F and G) and a large-area (2 cm by 2 cm pixel) PeLED (fig. S13B) were fabricated. Our study reduces the technical gap between PeLEDs and OLEDs or quantum dot LEDs and is a big step toward the development of efficient

next-generation emitters with high color purity and low fabrication cost based on perovskites.

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ACKNOWLEDGMENTS

This work was partially supported by Samsung Research Funding Center of Samsung Electronics under Project Number SRFC-MA-1402-07. A.S. was partially supported by the Engineering and Physical Sciences Research Council (UK). All data are available in the main text and the supplementary materials.

SUPPLEMENTARY MATERIALS

www.sciencemag.org/content/350/6265/1222/suppl/DC1
Materials and Methods
Supplementary Text
Figs. S1 to S13
Tables S1 to S5
References (35–43)

4 August 2015; accepted 22 October 2015
10.1126/science.aad1818

LASER PHYSICS

Ultraviolet surprise: Efficient soft x-ray high-harmonic generation in multiply ionized plasmas

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High-harmonic generation is a universal response of matter to strong femtosecond laser fields, coherently upconverting light to much shorter wavelengths. Optimizing the conversion of laser light into soft x-rays typically demands a trade-off between two competing factors. Because of reduced quantum diffusion of the radiating electron wave function, the emission from each species is highest when a short-wavelength ultraviolet driving laser is used. However, phase matching—the constructive addition of x-ray waves from a large number of atoms—favors longer-wavelength mid-infrared lasers. We identified a regime of high-harmonic generation driven by 40-cycle ultraviolet lasers in waveguides that can generate bright beams in the soft x-ray region of the spectrum, up to photon energies of 280 electron volts. Surprisingly, the high ultraviolet refractive indices of both neutral atoms and ions enabled effective phase matching, even in a multiply ionized plasma. We observed harmonics with very narrow linewidths, while calculations show that the x-rays emerge as nearly time-bandwidth-limited pulse trains of ~100 attoseconds.

High-order harmonic generation (HHG) results from the extreme quantum nonlinear response of atoms to intense laser fields: Atoms in the process of being ionized by an intense femtosecond laser pulse

coherently emit short-wavelength light that can extend well into the soft x-ray region (1–6). When implemented in a phase-matched geometry to ensure that the laser and HHG fields both propagate at the same speed $\sim c$, HHG from

many atoms adds constructively to generate bright, coherent beams (7). The high temporal coherence of HHG supports ultrabroad bandwidths ($\Delta\lambda/\lambda \approx 1$) that simultaneously span many characteristic elemental absorption edges, as well as pulse durations from femtoseconds to attoseconds (8–11), making it possible to capture the fastest electron dynamics in atoms, molecules, nanosystems, and materials (12–23). Moreover, the high spatial coherence of HHG makes it possible to image with spatial resolution near the wavelength limit (24, 25). Recently, the use of mid-infrared (IR) femtosecond driving lasers enabled the generation of bright x-ray supercontinua extending to photon energies greater than 1.6 keV (26).

To date, however, generating bright harmonics demanded a trade-off between two competing factors. High harmonics are radiated as a result of a laser-driven quantum-coherent electron recollision process that occurs while an atom is ionizing. This physics dictates that the HHG emission per atom is brightest for short-wavelength ultraviolet (UV) driving lasers, because the short laser cycle minimizes quantum diffusion of the electron wave packet as it propagates away from, and then back to, its parent ion. This maximizes the probability of the recollision HHG event and hence the HHG yield per atom (27). In contrast, generating and phase-matching HHG in the soft x-ray region favors long-wavelength, mid-IR lasers ($>0.8 \mu\text{m}$) (26, 28–30). This can be understood from simple arguments. First, the maximum HHG photon energy emitted by a single atom scales quadratically with laser wavelength and is given by $h\nu_{\text{SA}} \approx I_p + 3.17 U_p$ (4), where $U_p \propto I_L \lambda_L^2$ is the average quiver energy of the electron in a laser field of intensity I_L and wavelength λ_L . Second, phase matching is achieved by balancing the positive dispersion of the neutral gas with the negative contribution of the free electrons and is only possible for ionization levels of $<5\%$ for argon. Fortunately, the lower laser intensity required for long-wavelength driving lasers means that the medium is only weakly ionized, thereby enabling phase matching.

Very weak HHG emission at high photon energies of ~ 200 to 500 eV at very low (few torr) gas pressures has been observed using intense UV and near-IR lasers (1, 31, 32). In those studies, the HHG emission emerged from ionization of a small number of ions, which emit harmonics with comparable efficiency to neutral atoms (33). Moreover, the inability to phase-match the HHG

process in plasmas, combined with strong plasma-induced defocusing of the laser, meant that the HHG flux was weaker than theoretically possible in a phase-matched geometry by a factor of 10^{-4} to 10^{-11} .

Here, we demonstrate a regime of bright high-harmonic emission in multiply ionized plasmas

(Figs. 1 and 2). Using intense UV driving lasers at a wavelength of $0.27 \mu\text{m}$, bright discrete HHG peaks extend well into the soft x-ray region of the spectrum. It is well established that low quantum diffusion of the electron wave packet (due to the shorter time the electron spends away from the ion) maximizes the single-atom yield for UV

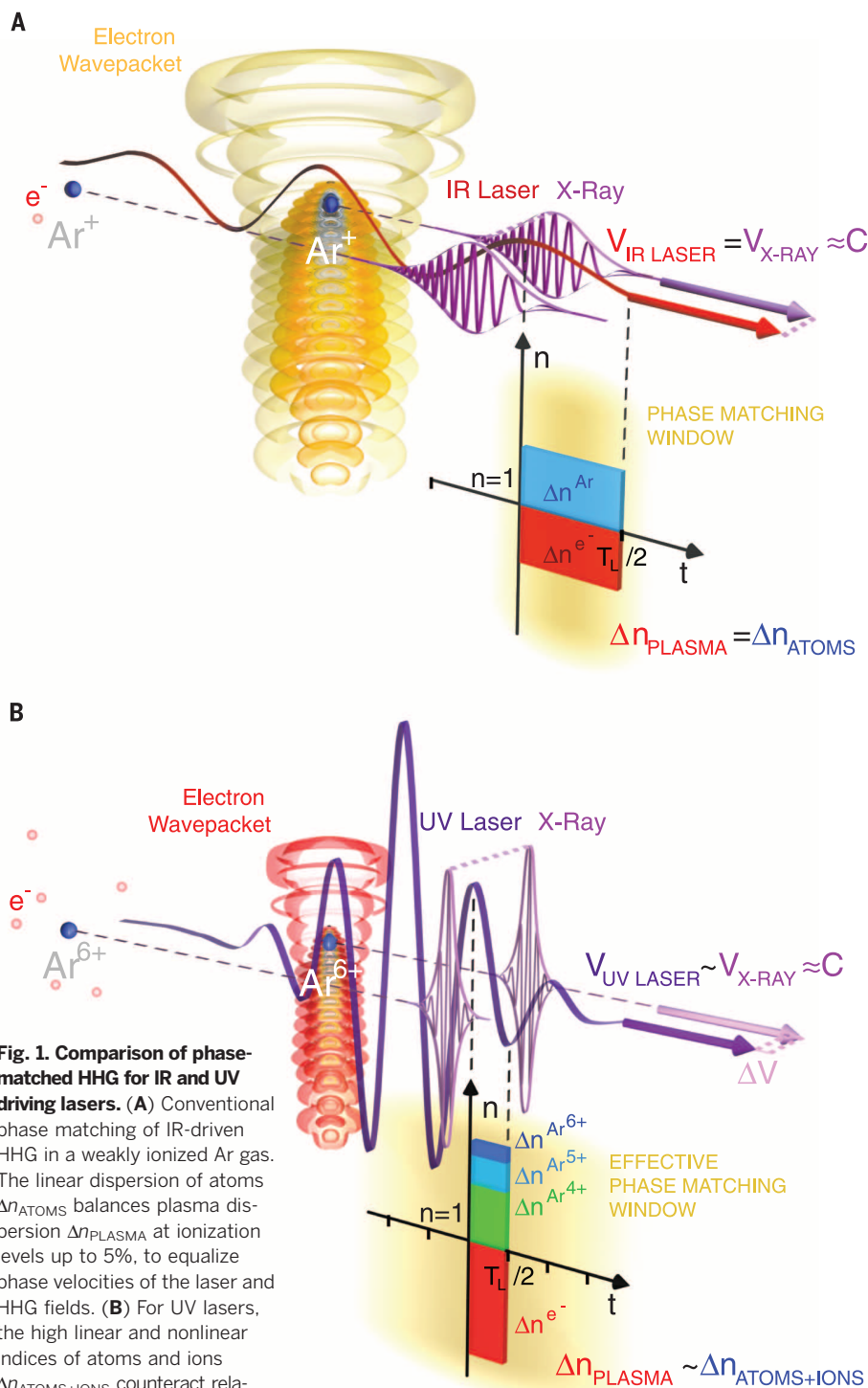


Fig. 1. Comparison of phase-matched HHG for IR and UV driving lasers. (A) Conventional phase matching of IR-driven HHG in a weakly ionized Ar gas. The linear dispersion of atoms Δn_{ATOMS} balances plasma dispersion Δn_{PLASMA} at ionization levels up to 5%, to equalize phase velocities of the laser and HHG fields. (B) For UV lasers, the high linear and nonlinear indices of atoms and ions

$\Delta n_{\text{ATOMS+IONS}}$ counteract relatively low plasma dispersion, ensuring a good HHG yield even in a multiply ionized plasma (500% ionization). Δv is the small offset from the speed of light c . The large single-atom yield, coupled with coherence lengths ranging from several micrometers to ∞ , as well as low harmonic orders, result in full to effective phase matching over many laser cycles.

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driving lasers. However, in this new regime of intense UV-driven HHG, the higher linear and nonlinear indices of atoms and ions contribute substantially to the dispersion experienced by the driving laser and serve to counteract plasma dispersion (Fig. 1B). This enables coherent build-up of the HHG signal in multiply ionized plasmas at very high gas pressures (i.e., effective phase matching) to photon energies greater than 280 eV, corresponding to harmonic orders of only ~ 61 .

We observed high conversion efficiencies of $\sim 10^{-3}$ to 10^{-7} throughout the extreme UV (EUV) and soft x-ray regions; these values are orders of magnitude brighter than has been observed to date from ions. The well-separated (~ 9 eV) narrowband HHG peaks, with linewidths of 70 to 700 meV ($\lambda/\Delta\lambda \approx 350$ to 450) in the vacuum UV (VUV) to soft x-ray regions, are ideal for applications in imaging and photoelectron spectroscopies. The high HHG efficiency and narrow linewidths arise from a long phase-matching window as well as low group velocity walk-off, so that group and phase velocity matching are possible over many laser cycles. Moreover, in contrast to the strongly chirped HHG emission driven by near- and mid-IR driving lasers, simulations show that UV-driven harmonics emerge as nearly time-bandwidth-limited series of ~ 100 -as bursts. Our predictions indicate that bright UV-driven harmonics can extend into the multi-keV region. This leads to the surprising conclusion that the fundamental of Ti:sapphire lasers may be the most limited for generating bright soft x-ray harmonics, relative to using longer- or shorter-wavelength driving lasers.

In our experiment, high harmonics were produced by focusing the third harmonic (0.27 μm) of a Ti:sapphire laser into an Ar-filled waveguide (diameter 150 to 400 μm , length 1 to 15 mm) at pressures between 1 and 1500 torr (see supplementary materials). The pulse energy and duration were 2.6 mJ and 35 fs [full width at half maximum (FWHM)], respectively. By focusing to a spot size less than 55 μm in diameter, the peak laser intensity was $>6 \times 10^{15}$ W/cm 2 , with a confocal parameter less than 17 mm.

Figure 2A shows that bright HHG emission from Ar extends far beyond the ~ 30 -eV limit predicted using only the dispersion of atoms, to photon energies of >280 eV (see fig. S1 for HHG plotted on a linear scale). The high laser intensity required for UV-driven soft x-ray HHG (at $>6 \times 10^{15}$ W/cm 2) is well above the barrier suppression ionization for atoms; thus, neutral atoms will be fully ionized well before the peak intensity of the pulse. However, this intensity is in the tunneling regime for ions. Moreover, time-dependent Schrödinger equation (TDSE) calculations (Fig. 2B and fig. S3) show that HHG from Ar in this energy range must emerge from ions (Ar $^+$ to Ar $^{5+}$) with relatively high ionization potentials ($I_p^{\text{Ar}^+} = 27.6$ eV to $I_p^{\text{Ar}^{5+}} = 90.1$ eV).

Phase matching in UV-driven VUV and soft x-ray HHG optimizes at higher gas pressures of ~ 100 to 400 torr, as shown in Fig. 2A, fig. S1,

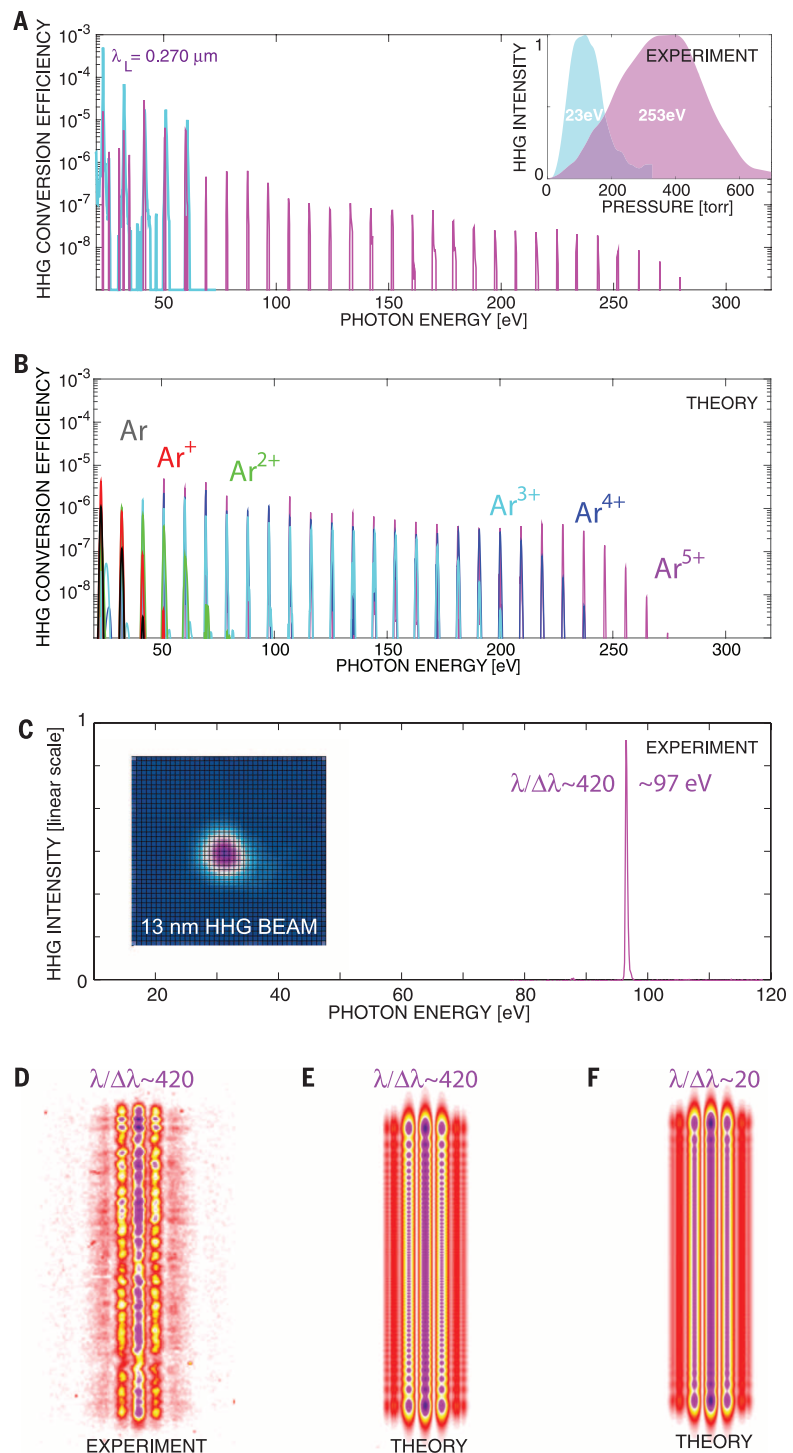


Fig. 2. UV-driven HHG gives bright discrete peaks and isolated harmonics into the soft x-ray region.

(A) Experimentally observed UV-driven HHG from multiply ionized Ar, optimized in the EUV (blue spectrum) and soft x-ray (purple spectrum) regions. Inset: VUV HHG optimizes at <100 torr and low laser intensities ($>10^{15}$ W/cm 2), while soft x-ray HHG optimizes at 400 torr and high intensities ($>6 \times 10^{15}$ W/cm 2). (B) Predicted HHG yield from single Ar atoms and ions using TDSE calculations. Above 30 eV, the extended UV-driven HHG must originate from highly charged ions. The emission from different ionic species is plotted separately (not integrated). (C) Experimentally isolated 13-nm harmonic with ultranarrow linewidth of $\lambda/\Delta\lambda \approx 420$ or 230 meV. Adjacent harmonic orders were eliminated using Rh + Si + Be filters. The inset shows the 13-nm HHG beam. (D to F) Experimental and theoretical Young's double-slit diffraction patterns showing full spatial coherence, from a slit of width of 20 μm and height 1.5 mm. The spatial modulations perpendicular to the slit in (D) and (E) are due to the high spectral purity that generates observable interferences in (D). For broad harmonic linewidths (F), the vertical spatial modulations are not present.

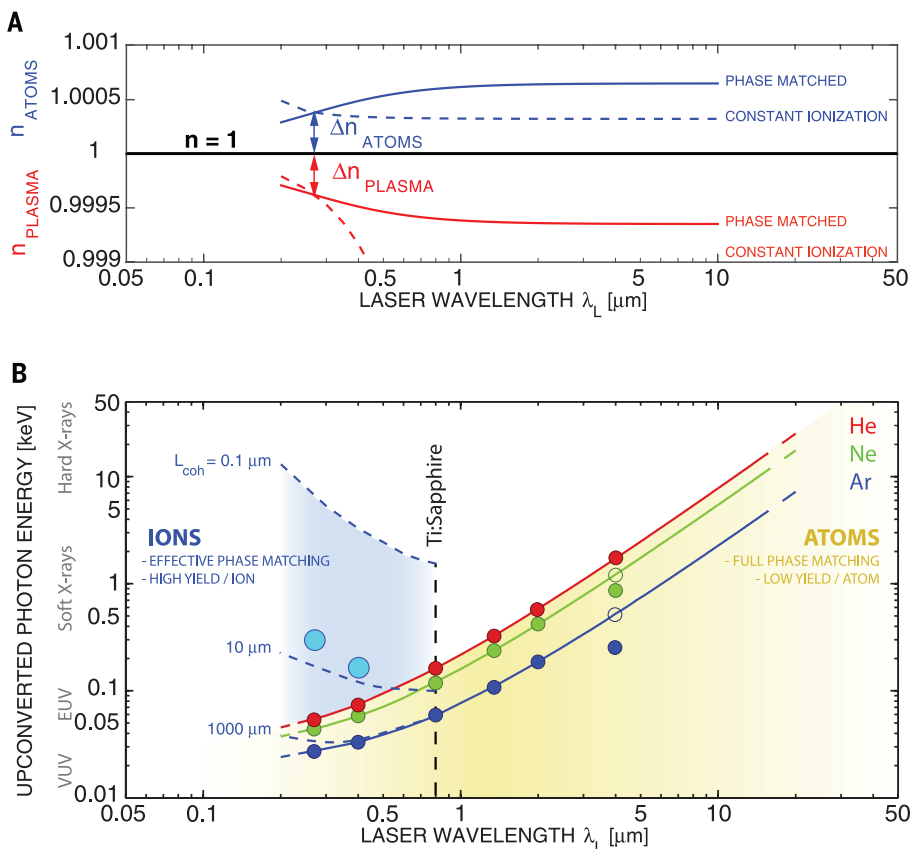


Fig. 3. Phase matching of HHG using UV to mid-IR lasers. (A) Refractive index of Ar atoms (blue dashed) compared with that of free electron plasma (red dashed) as a function of wavelength, for constant ionization conditions of 40%. The solid lines plot the indices under phase-matching conditions near cutoff, where IR-driven HHG needs multi-atmospheres of gently ionized gas, whereas UV-driven HHG occurs in a multiply ionized plasma. (B) Bright HHG from atoms and ions for UV to mid-IR driving lasers. The experimental data are plotted as circles. The solid lines plot the theoretical full phase-matching limits, including only the index of neutral atoms. The dashed lines also include the refractive indices of ions, which extend UV-driven HHG effective phase matching into the soft x-ray region.

and table S1. This is in contrast to all previous observations of HHG x-rays from ions in a non-phase-matched regime, where very high harmonic orders can be observed only at pressures that are lower by about two orders of magnitude (1 to 3 torr) (31, 33). In general, only harmonic orders that are phase-matched will increase in intensity with increasing gas pressure. The optimal pressures increase with harmonic order to compensate for increasing plasma dispersion. Furthermore, the increasing HHG yield with pressure indicates that ionization-induced defocusing of the laser is not a dominant limitation. Other evidence of good coherent HHG signal buildup over many laser cycles is the narrow spectral width of UV-driven HHG, shown in Figs. 1 and 2 and fig. S1. The linewidths decrease from >900 meV (at ~50 eV) for Ti:sapphire lasers, to ~70 meV (at ~30 eV) and 400 meV (at ~180 eV) for UV driving lasers. These narrow-linewidth HHG peaks, with spectral purity up to $\lambda/\Delta\lambda > 450$, are observed despite strong ionization that must occur on the leading edge of the driving laser pulse and that would normally result in strong spectral broadening and blue shifting of both the driving

laser and HHG emission. Fortunately, because this frequency shift scales as $\Delta\lambda_{\text{LASER}} \sim -\lambda_{\text{LASER}}^3$ at similar rates of ionization (34, 35), this shift is smaller for UV lasers, which preserves narrow harmonic linewidths.

Because the HHG spectra consist of odd-harmonic peaks that are well separated in energy (>9 eV), UV-driven HHG also provides a practical way to isolate a single harmonic order. Figure 2 plots a single harmonic near the technologically relevant 13.5-nm wavelength for lithography, highlighting the excellent beam quality (Fig. 2C, inset) and high spatial and temporal coherence. Lower harmonic orders were eliminated by the same thin-film filters used to reject the fundamental laser light, whereas higher cutoff harmonics were excluded by adjusting the intensity of the UV laser. Figure 2, D to F, plots the experimental and theoretical double-slit diffraction patterns for a slit of width 20 μm , slit separation of 50 μm , and height of 1.5 mm. The spatial modulations perpendicular to the slit in Fig. 2, D and E, are due to the high spectral purity of the HHG beam and generate observable interference both along and perpendicular to the slit.

At 13 nm, the estimated HHG flux of Fig. 2C corresponds to $>10^{11}$ photons/s (peak brightness $>10^{29}$ photons $\text{s}^{-1} \text{mm}^{-2} \text{mrad}^{-2}$) at the exit of the waveguide under optimal conditions for generating 280-eV harmonics. Over the whole spectral range, the efficiencies into a single harmonic order are estimated to approach 10^{-3} to 10^{-7} in the VUV, EUV, and soft x-ray regions. The HHG flux was measured to be consistent using three different methods. First, we compared HHG driven by 0.8- μm and 0.27- μm lasers in the same spectral region. Second, we estimated the efficiency from known spectrometer, x-ray filter, and charge-coupled device efficiencies. Third, we used a NIST-calibrated vacuum diode to measure the flux in the VUV and EUV regions. We observed good HHG signal—comparable to or greater than phase-matched HHG at 100 eV driven by 0.8- μm lasers—throughout the EUV and soft x-ray regions (Fig. 2 and fig. S1).

High harmonics were first observed in 1987 using a UV driving laser (1). That work used longer pulses (by a factor of ~10) in a tight focus geometry, and HHG up to 85 eV (14.6 nm) was observed with estimated efficiency of 10^{-11} . Subsequent work observed HHG from ions (also using long-pulse UV lasers in a tight focus geometry with limited interaction length), with conversion efficiencies around 10^{-10} or 10^{-12} at photon energies from 100 to 180 eV (32). More recently, broadband HHG from Ar ions up to 500 eV was observed for 0.8- μm driving lasers in a few-torr gas-filled hollow waveguide (31). However, this emission was also extremely weak because of the low pressures (few torr) and poor phase-matching conditions (see table S1 for comparison).

To quantitatively explain why bright harmonics from Ar driven by UV lasers can extend into the soft x-ray region, we used simple numerical models, which have been extensively validated for near and mid-IR driving lasers, as well as exact integration of the time-dependent Schrödinger equation (26, 28–30). To aid with physical insight, Fig. 3A (dashed lines) plots the calculated index of refraction contribution of an Ar atom compared with that of a free electron. As expected, the refractive indices of neutral atoms are largest in the UV region of the spectrum.

On the other hand, the free electron plasma contribution to the refractive index scales as $n_{\text{plasma}} = [(1 - \omega_p^2)/\omega_{\text{LASER}}^2]^{1/2}$, where $\omega_p = (n_e e^2/m_e \epsilon_0)^{1/2}$ is the plasma frequency corresponding to an electron density n_e , and where e and m_e are the charge and mass of the electron. Hence, lower frequencies (i.e., longer laser wavelengths) will experience much higher plasma dispersion, and therefore phase matching occurs only at low ionization levels below the critical ionization (7, 36) (table S1).

In contrast, for wavelengths in the visible and UV spectral regions, the positive refractive index contribution of a neutral Ar atom exceeds the negative contribution of a free electron. This corresponds to a critical ionization level of ~40% for UV-driven HHG at ~40 eV. Moreover, the

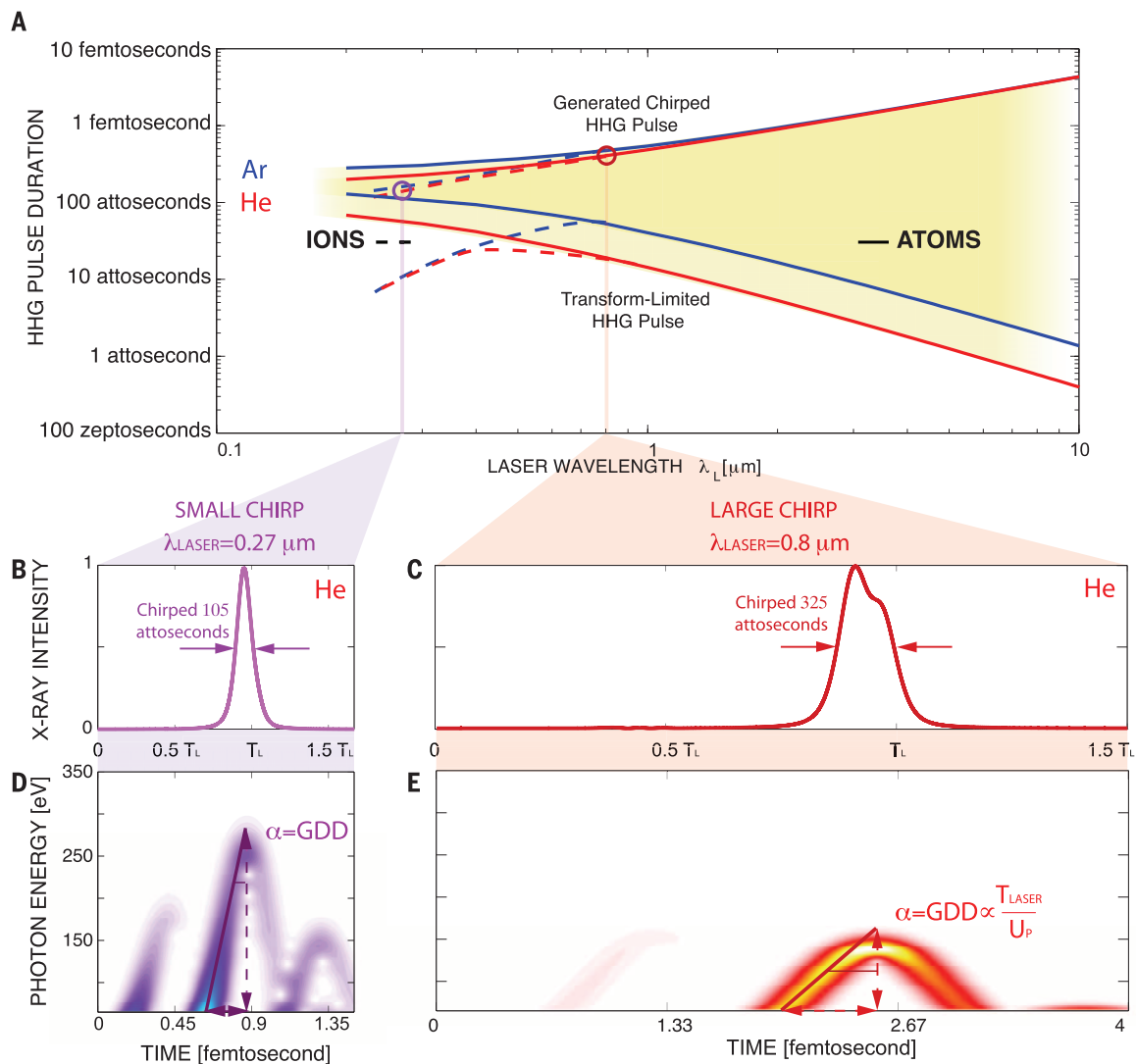


Fig. 4. Theoretical UV-driven HHG gives shorter duration and lower chirp pulses than mid-IR-driven HHG. (A) The pulse duration of HHG soft x-ray bursts converges to the transform limit for UV driving lasers. (B to E) Chirp [group delay dispersion (GDD)] of the HHG pulses in He driven by intense three-cycle UV and near-IR lasers, respectively. For UV lasers, the HHG chirp is reduced as a result of the shorter laser cycle duration T_{LASER} and

the higher ponderomotive potential U_P (higher HHG cutoff). The highest harmonics with a 280-eV cutoff (spectrally filtered by a Rh thin film) have a pulse duration of 105 as (even shorter 45- to 75-as pulses could be generated from He and He⁺; see supplementary materials). In comparison, for a 0.8- μm driver and a phase-matching cutoff of 160 eV, the pulse durations are 325 as (>3 times as long).

refractive indices of ions in the UV are comparable to that of neutral Ar (see supplementary materials), as the ionization potential of each successive ionization stage increases only modestly. Thus, for UV driving lasers, good buildup of the HHG signal is possible even in a multiply ionized plasma. This enables extension of effective phase matching into the soft x-ray region and, in theory, even to hard x-rays. Note that for UV-driven HHG, full phase matching is possible in the VUV-EUV, while efficient HHG is possible in soft x-ray region at high pressures, with high photon flux.

In our simple phase-matching model, we consider a one-dimensional geometry, which corresponds to the general case of a large waveguide diameter or large focal spot size (near-plane wave propagation). To calculate the phase mis-

match to a first approximation, we need to consider a generalized set of multispecies time-dependent equations, given by

$$\begin{aligned} \Delta k(t) &= qk_{\omega}(t) - k_{q\omega}(t) \\ &\approx \underbrace{-qP\eta_0(t) \frac{2\pi}{\lambda_L} [\delta_L^0(t) + \tilde{n}_2^0(t)I_L(t)]}_{\text{neutral atoms}} \\ &\quad - \underbrace{\sum_{i=1,2,\dots} qP\eta_i(t) \frac{2\pi}{\lambda_L} [\delta_L^i(t) + \tilde{n}_2^i(t)I_L(t)]}_{\text{multiply charged atoms}} \\ &\quad + \underbrace{qP\eta_{\text{total}}(t)N_{\text{atm}}r_e\lambda_L + \Delta k_{\text{geometry}}}_{\text{free electrons}} \quad (1) \end{aligned}$$

where $\eta_i(t)$ is the fractional population of the various gas species present at a given moment ($i=0$ denotes

neutral atoms, $i=1, 2, 3, \dots$ denote various ion states), $\eta_{\text{total}}(t)$ is the cumulative fractional ionization [$\eta_{\text{total}}(t) > 100\%$ for multiply charged ions], r_e is the classical electron radius, N_{atm} is the number density of atoms at 1 atm, P is the pressure, and $\delta_L^i(t)$ is the difference between the indices of refraction at the fundamental and harmonic wavelengths (which is very large in the UV). Although in general the nonlinear index contributions are estimated to play a rather small role, for high UV laser intensities $> 6 \times 10^{15} \text{ W/cm}^2$, an additional term due to the nonlinear index of refraction (t) must also be included, estimated by multiconfigurational self-consistent field calculations (table S2). For $\eta_{\text{total}}(t) > 10\%$, one must include the dispersion of ions as well as a cumulative total ionization level η_{total} resulting from all ions of higher charge. The phase-matching photon energy limits

are determined by the ionization level at which a dispersion balance is achieved and are independent of HHG geometry (the geometrical dispersion sets only an optimal pressure for a wave-guiding geometry) (7, 29). For our experimental conditions, at any time during the HHG emission, two to three species contribute strongly to the HHG signal (Fig. 2B and fig. S2). Fortunately, for a given HHG photon energy, the harmonic order q is lower for UV-driven versus mid-IR-driven HHG, naturally leading to longer coherence lengths even at very high ionization levels and pressures as $\Delta k \propto q$.

Figure S6 plots the estimated dynamic phase mismatch ratio due to plasma and to atoms and ions for Ar driven by 10-cycle 0.27- and 0.8- μm lasers. The dashed black horizontal lines show the high-flux HHG region with coherence lengths $L_{\text{coh}} = \pi/\Delta k$ from infinity to 10 μm . This time window is substantially longer for UV driving lasers than for near-IR driving lasers, extending effective phase matching over ~ 5 to 40 half-cycles or a time interval of ~ 2 to 18 fs. This picture is also consistent with the observed narrow spectral linewidths in the VUV to x-ray regime at high phase-matching pressures (Fig. 2 and fig. S1). Under our conditions, at a photon energy of 250 eV, $L_{\text{coh}} > 3 \mu\text{m}$, the absorption length $L_{\text{abs}} \approx 1 \text{ mm}$ at 400 torr (for ions see fig. S7), whereas the medium length $L_{\text{med}} \approx 1$ to 15 mm. At 40 eV, $L_{\text{coh}} \approx \infty$.

Additional nonlinear effects—for example, due to laser pulse self-guiding or filamentation, which are likely present—would further enhance effective HHG phase matching in plasmas, because the nonlinear index induced by the laser will increase further to compensate for plasma-induced dispersion. Figure S10 shows blue-shifting and broadening of the fundamental spectrum that is characteristic also for self-effects in efficient HHG at other laser wavelengths, at 0.8 μm and in the mid-IR phase-matching regimes (26, 31, 37). This is also supported by our observation that in a short gas cell geometry the HHG spectrum extends to only ~ 180 eV in Ar, Ne, or He.

Decreased medium opacity due to removal of several valence electrons can also increase the yield, particularly for intense UV-driven HHG, where the single-atom yield is already very high. However, we calculate that increasing transparency of the medium is not sufficient to explain the observed increase in HHG yield, especially when the coherence length is smaller than the absorption length. As shown in fig. S6, while the transparency increases as expected at photon energies around 100 eV, in the soft x-ray region the transparency does not change substantially. Thus, in the future, all-optical quasi-phase-matching HHG techniques could be applied to take advantage of the full x-ray absorption length to enhance the yield further (38–41).

We also modeled UV-driven HHG using the TDSE. Figure 2B plots the TDSE predictions for strong field ionization in Ar for a peak laser intensity similar to the experiment, which shows that HHG in the 30- to 280-eV photon energy range must be generated from multiply ionized

species, up to Ar^{5+} , at ionization levels above 500% (on axis of the waveguide). This far exceeds the 5% critical ionization limit for fully phase-matched HHG in Ar using 0.8- μm lasers. Our TDSE calculations show that the single-atom yield scales more strongly than $\sim \lambda_L^{-7.5}$ (42) for a single harmonic of He, corresponding to a factor of ~ 4000 greater yield for 0.27- μm relative to 0.8- μm driving lasers. A similar scaling is expected for Ar species, although with a slightly modified exponent.

These TDSE calculations also show that HHG driven by UV is particularly suitable for generating nearly transform-limited isolated attosecond bursts (or pulse trains), with very low temporal chirp that should be straightforward to compensate. It is already known that the atto-chirp of each individual attosecond burst will be reduced as the driving laser wavelength is reduced in the UV, because of the shorter time the electron spends in the continuum (~ 300 as). However, for higher photon energies using more intense UV driving lasers, the pulse duration and atto-chirp will be reduced even further as a result of the larger phase-matched bandwidth (i.e., large U_p). Figure 4 plots a time-frequency analysis for HHG in He driven by intense three-cycle UV and 0.8- μm lasers, where the reduction in the temporal chirp is very apparent. This effect is dictated by the duration of an individual laser cycle, independent of the number of cycles in the laser pulse. In the case of UV driving lasers, the FWHM duration of the highest harmonics naturally emerges as slightly chirped ~ 105 -as bursts, compared with strongly chirped 325-as pulses for an 0.8- μm driving laser in the same photon energy range. For comparison, for 2- to 4- μm mid-IR-driven HHG, the emission is brightest when the HHG pulse emerges as an isolated, very strongly chirped, 300- to 1200-as burst (26). The experimental HHG emission from Ar is predicted to emerge as a long 10-fs train of nearly transform-limited ~ 100 -as pulses.

Another advantage of UV driving lasers is the low group velocity walk-off. This is in contrast to mid-IR ($>2 \mu\text{m}$)-driven HHG, where group velocity walk-off limits the coherent buildup length and conversion efficiency (29, 43). Using UV lasers, the temporal window for phase matching increases while the walk-off decreases (see supplementary materials). Both the group and phase velocities of the driving laser and HHG light can be nearly matched, so that the electron wave packets of different atoms in the medium rescatter in a coherent way (i.e., electron wave packets have the same quantum paths and same quantum phases, resulting in highly temporally coherent HHG). Furthermore, because the coherence length for effective phase matching in the soft x-ray region is smaller than the characteristic group velocity walk-off length (see supplementary materials and table S1), intense UV-driven HHG is also effectively group velocity-matched

As shown in Fig. 3B, our best current experimental and theoretical understanding indicates that shorter UV laser wavelengths and

intensities $>10^{16} \text{ W/cm}^2$ will produce bright HHG emission at even higher soft x-ray photon energies $\gg 280$ eV, which would be ideal for coherent imaging. The phase mismatch decreases more slowly using UV lasers compared with near-IR or mid-IR lasers; this is due to the lower harmonic orders and pressures required (i.e., lower q and P in Eq. 1). To a first approximation under ideal phase-matching conditions, every term in Eq. 1 scales linearly with the laser wavelength. Because lower harmonic orders correspond to much higher photon energies in the case of UV driving lasers, the coherence length is relatively long compared to the coherence length at the same photon energy generated with a longer-wavelength UV-visible laser (Fig. 3B). This ensures strong constructive buildup over the interaction region in an effectively phase-matched geometry even in the presence of a finite phase mismatch—and also ensures HHG emission that is as bright as fully phase-matched HHG at 13 nm in He driven by 0.8- μm lasers. This strongly contrasts with longer-wavelength mid-IR lasers, where the order of the upconversion process is higher, with $q > 5000$ for a 4- μm driver.

Using intense UV driving lasers, effective phase matching of the HHG process extends the bright emission in the VUV, EUV, and soft x-ray regions. This regime provides coherent light with contrasting and complimentary spectral and temporal properties, compared to the mid-IR-driven HHG x-rays: These exhibit ultrabroad super-continuum spectra that can be used to probe multiple elements over a spectral range of >1 keV. Remarkably, the UV-driven HHG linewidths decrease to fractional bandwidths of $\lambda/\Delta\lambda \approx 450$ that are ideal for a complementary set of scientific and technological applications, such as in photoemission spectroscopy with very high energy resolution and coherent diffraction imaging with very high spatial resolution (44, 45). In terms of laser technology, the availability of intense femtosecond UV lasers (e.g., harmonics of Yb:YAG, Ti:sapphire, or excimer lasers) makes this approach ideal for many applications. Finally, there is a strong potential to produce much brighter HHG beams at even higher multi-keV x-ray photon energies than would be possible with other approaches.

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ACKNOWLEDGMENTS

The experimental work was done at JILA, supported by Army Research Office grant WN11NF-13-1-0259, an NSF PFI AIR award, and U.S. Department of Energy (DOE) grant DE-SC0008803 (M.M.M., T.P., and H.C.K.). Theory was supported by a Marie Curie International Outgoing Fellowship within the EU Seventh Framework Programme for Research and Technological Development (2007–2013) under REA

grant agreement 328334 (C.H.-G.); Junta de Castilla y León (SA116U13, UI0016) and MINECO (FIS2013-44174-P) (C.H.-G. and L.P.); NSF grants PHY-1125844 and PHY-1068706 and AFOSR MURI “Mathematical Modeling and Experimental Validation of Ultrafast Light-Matter Coupling associated with Filamentation in Transparent Media” grant FA9550-10-1-0561 (A.J.-B., R.J.L., X.G., A.L.G., M.M.M., and H.C.K.); Ministry of Science and Technology, Taiwan, grant 102-2112-M-007-025-MY3 (M.-C.C.); U.S. Department of Energy, Division of Chemical Sciences, Atomic, Molecular and Optical Sciences Program (A.B.); and DOE Office of Fusion Energy, HED Laboratory Plasmas program, grant AT5015033 (S.B.L., M.F., and J.A.G.). Lawrence Livermore National Laboratory is operated by Lawrence Livermore National Security LLC for DOE, National Nuclear Security Administration, under contract DE-AC52-07NA27344, LLNL-JRNL-676693. T.P., D.P., M.M.M., and H.C.K. have filed a patent on “Generation of VUV, EUV, X-ray Light Using VUV-UV-VIS Lasers.” U.S. patent application 61873794 (2013)/US 20150063385 (2015).

SUPPLEMENTARY MATERIALS

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Supplementary Text
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7 July 2015; accepted 19 October 2015
10.1126/science.aac9755

QUANTUM HALL EFFECT

Evidence for a fractional fractal quantum Hall effect in graphene superlattices

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The Hofstadter energy spectrum provides a uniquely tunable system to study emergent topological order in the regime of strong interactions. Previous experiments, however, have been limited to low Bloch band fillings where only the Landau level index plays a role. We report measurements of high-mobility graphene superlattices where the complete unit cell of the Hofstadter spectrum is accessible. We observed coexistence of conventional fractional quantum Hall effect (QHE) states together with the integer QHE states associated with the fractal Hofstadter spectrum. At large magnetic field, we observed signatures of another series of states, which appeared at fractional Bloch filling index. These fractional Bloch band QHE states are not anticipated by existing theoretical pictures and point toward a distinct type of many-body state.

In a two-dimensional electron gas (2DEG) subjected to a magnetic field, the Hall conductivity is generically quantized whenever the Fermi energy lies in a gap (I). The integer quantum Hall effect (IQHE) results from the cyclotron gap that separates the Landau energy levels (LLs). The longitudinal resistance drops to zero, and the Hall conductivity develops plateaus

quantized to $\sigma_{XY} = \nu e^2/h$, where ν , the Landau level filling fraction, is an integer; h is Planck’s constant; and e is the electron charge. When the 2DEG is modified by a spatially periodic potential, the LLs develop additional subbands separated by minigaps, resulting in the fractal energy diagram known as the Hofstadter butterfly (2). When plotted against normalized magnetic flux ϕ/ϕ_0 and normalized density n/n_0 (representing the magnetic flux quanta and electron density per unit cell of the superlattice, respectively), the fractal minigaps follow linear trajectories (3) according to a Diophantine equation, $n/n_0 = t\phi/\phi_0 + s$, where s and t are integers; s is the Bloch band-filling index associated with the superlattice, and t is a similar index related to the gap structure

along the field axis (4) (in the absence of a superlattice, t reduces to the LL filling fraction). The fractal minigaps give rise to QHE features at partial Landau level filling, but in this case t , rather than the filling fraction, determines the quantization value (I , 5) and the Hall plateaus remain integer-valued.

In very-high-mobility 2DEGs, strong Coulomb interactions can give rise to many-body gapped states also appearing at partial Landau fillings (6–8). Again, the Hall conductivity exhibits a plateau, but in this case quantized to fractions of e^2/h . This effect, termed the fractional quantum Hall effect (FQHE), represents an example of emergent behavior in which electron interactions give rise to collective excitations with properties fundamentally distinct from the fractal IQHE states. A natural theoretical question arises regarding how interactions manifest in a patterned 2DEG (9–12). In particular, because both the FQHE many-body gaps and the single-particle fractal minigaps can appear at the same filling fraction, it remains unclear whether the FQHE is even possible within the fractal Hofstadter spectrum (13–15). Experimental effort to address this question has been limited, owing to the requirement of imposing a well-ordered superlattice potential while preserving a high carrier mobility (16–18).

Here, we report a low-temperature magnetotransport study of fully encapsulated hexagonal boron nitride (h-BN)/graphene/h-BN heterostructures, fabricated by van der Waals assembly with edge contact (19, 20). A key requirement to observe the Hofstadter butterfly is the capability to reach the commensurability condition in which the magnetic length $l_B = \sqrt{\hbar/eB}$ (where \hbar is Planck’s constant divided by 2π , e is the electron charge, and B is the magnetic field) is comparable to the wavelength of the spatially periodic potential, λ . For experimentally accessible magnetic

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Ultraviolet surprise: Efficient soft x-ray high-harmonic generation in multiply ionized plasmas

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Science **350** (6265), 1225-1231.
DOI: 10.1126/science.aac9755

Short wavelengths birth shorter ones

The shortest laser pulses—with durations measured in attoseconds—arise from a process termed high-harmonic generation (HHG). Essentially, a longer, "driving" pulse draws electrons out of gaseous atoms like a slingshot, and, when they ricochet back, light emerges at shorter wavelengths. Most HHG has been carried out using light near the visible/infrared boundary for the driving pulse. Popmintchev *et al.* used an ultraviolet driving pulse instead, which yielded an unexpectedly efficient outcome. These results could presage a more generally efficient means of creating x-ray pulses for fundamental dynamics studies as well as technological applications.

Science, this issue p. 1225

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